



Article Upconversion Luminescence from Sol-Gel-Derived Erbium- and Ytterbium-Doped BaTiO₃ Film Structures and the Target Form

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Abstract: Sol-gel technology has attracted attention in the fabrication of diverse luminescent materials and thin film structures, with forms that range from powders to microcavities. The optical properties of sol-gel-derived structures depend on the sol composition, deposition, and heat treatment conditions, as well as on the film thicknesses and other factors. Investigations on the upconversion luminescence of lanthanides in film structures and materials are also ongoing. In this study, we synthesized three different types of materials and film structures using the same sol, which corresponded to a $Ba_{0.76}$ Er_{0.04}Yb_{0.20}TiO₃ xerogel, as follows: (a) the target form, which used the explosive compaction method for sol-gel-derived powder; (b) single-layer spin-on xerogel films annealed at 450 and 800 °C; and (c) microcavities with an undoped $SiO_2/BaTiO_3$ Bragg reflector surrounding a Ba_{0.76}Er_{0.04}Yb_{0.20}TiO₃ active layer. The BaTiO₃:(Er,Yb)/SiO₂ microcavity exhibited an enhancement of the upconversion luminescence when compared to the BaTiO3:(Er,Yb) double-layer film fabricated directly on a crystalline silicon substrate. The reflection spectra of the BaTiO₃:(Er, Yb)/SiO₂ microcavity annealed at 800 $^{\circ}$ C demonstrated a deviation of the maxima of the reflection within 15% for temperature measurements ranging from 26 to 120 °C. From the analyses of the transmission and reflection spectra, the optical band gap for the indirect optical transition in the single layer of the BaTiO₃:(Er,Yb) spin-on film annealed at 450 °C was estimated to be 3.82 eV, while that for the film annealed at 800 °C was approximately 3.87 eV. The optical properties, upconversion luminescence, and potential applications of the BaTiO3:(Er,Yb) sol-gel-derived materials and structures are discussed in this paper.

Keywords: barium titanate; erbium; ytterbium; upconversion; luminescence; sol-gel; xerogel; microcavity; powder; refractive index; optical band gap



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1. Introduction

Over the past several decades, there has been a growing interest in the development of technologies for the fabrication of barium titanate targets and thin film structures [1]. High dielectric constants, low dissipation factors, large electro-optical coefficients, high breakdown voltages, and other attractive properties stimulate the application of diverse technologies for the fabrication barium titanate powders, ceramic targets, and thin films [2–14]. The deposition technologies for BaTiO₃ in a vacuum, as well those for as sol-gel synthesis, were used to fabricate thin film capacitors [4], electro-optical devices [5,6], optical IR filters [7], photonic crystals [8,9], and microcavities [10,11]. In addition, the strong luminescence of lanthanides in BaTiO₃ host materials is currently being widely investigated, particularly, Stokes luminescence under visible and UV light excitation [2,11] and upconversion photoluminescence (PL) excited under IR range illumination [12–14].

Recently, we reported on the sol-gel synthesis and optical properties of $BaTiO_3/SiO_2$ Bragg reflectors and microcavities [10]. In this work, we have presented data on upconversion luminescence from a sol-gel derived $BaTiO_3$ target doped with Er and Yb, i.e., a rare-earth-doped $BaTiO_3$:(Er,Yb) material, and we continued our investigation of the optical properties of $BaTiO_3/SiO_2$ microcavities annealed at temperatures ranging from 450 to 800 °C. We observed an enhancement of the upconversion luminescence in the microcavities with $BaTiO_3$:(Er,Yb) active layers, as well as the stable upconversion luminescence in the target material over the year and the significant changes in the amplitudes of the reflection spectra of the $BaTiO_3/SiO_2$ microcavities annealed at 800 °C. From the transmission and reflection spectra of the $BaTiO_3$:(Er,Yb) layer, we determined the refractive index, absorption index, optical band gap, and Urbach energy for the $BaTiO_3$:(Er,Yb) films annealed at 450 and 800 °C.

2. Experimental

2.1. Film Structures on Silicon and Fused Silica

Three types of sol were prepared for the synthesis of sol-gel-derived film structures and the target structure. For the synthesis of the barium titanate sol (sol I), titanium isopropoxide (Ti(OC₃H₇)₄) (97%, Sigma-Aldrich, Steinheim, Germany), barium acetate (Ba(CH₃COO)₂) (ACS reagent 99%, Sigma-Aldrich, Steinheim, Germany), acetylacetone (CH₃COCH₂COCH₃) (analytical grade, AO Vekton, Saint Petersburg, Russia), and acetic acid (CH₃COOH) were used as the starting components. The amounts of titanium isopropoxide and barium acetate were chosen so that the Ti/Ba ratio corresponded to the stoichiometric composition of the barium titanate in the films (i.e., Ti:Ba = 1:1). The mixture was stirred for 1 h with an electromechanical stirrer until all components were completely dissolved, resulting in a stable film-forming sol.

Sol II was prepared using the following procedure [10] for the synthesis of the BaTiO₃:(Er,Yb) xerogel, namely, Ba_{0.76}Er_{0.04}Yb_{0.20}TiO₃. Two solutions were prepared. The solution using titanium isopropoxide (Ti(OC₃H₇)₄) (97%, Sigma-Aldrich, Steinheim, Germany) in acetylacetone (CH₃COCH₂COCH₃) (analytical grade, AO Vekton, Saint Petersburg, Russia) was stirred until it cooled. Separately, barium acetate (Ba(CH₃COO)₂) (ACS reagent 99%, Sigma-Aldrich, Steinheim, Germany) was dissolved in distilled water and stirred until completely dissolved. Erbium acetate hydrate (Er(CH₃COO)₃·xH₂O) (99.9% trace metal basis, Sigma-Aldrich, Milwaukee, USA) was added to the barium acetate solution and stirred until complete dissolution. Then, ytterbium acetate hydrate (Yb(CH₃COO)₃·xH₂O) (99.95% trace metal basis, Sigma-Aldrich, Milwaukee, WI, USA) was added to the solution of barium and the erbium acetates and stirred until completely dissolved. Acetic acid (CH₃COOH) was added to the solution of Ba, Er, and the Yb acetates and stirred for approximately 5 min. Finally, the solutions of titanium isopropoxide and Ba, Er, and the Yb acetates were mixed and stirred for approximately 5 min. Ethanol (C₂H₅OH) was then added to this solution, which was then further stirred for 1.5 h.

To obtain silica xerogel (SiO₂), silica sol (sol III) was prepared. Concentrated nitric acid (HNO₃) (66%, reagent grade, Minimed, Bryansk, Russia) was added to an alcohol–water

mixture (the volume ratio of distilled water and ethanol (C₂H₅OH) was approximately 1:6) until the solution reached a pH of 1. Tetraethyl orthosilicate (Si(OC₂H₅)₄) (\geq 99.0% (GC), Sigma-Aldrich, Buchs, Switzerland) was added to this mixture and stirred, and the pH was adjusted again to 1 by adding concentrated nitric acid. The final solution was stirred for half an hour. The sol should be aged for at least 24 h in airtight conditions before deposition.

The sample representing a microcavity (BaTiO₃:(Er,Yb)/SiO₂ microcavity) was prepared by deposition wherein the sols were spun on a monocrystalline silicon substrate. After the deposition of sol I, it was dried at 200 °C for 10 min and annealed at 450 °C for 30 min. Then, sol III was deposited on the BaTiO₃ xerogel layer and subjected to the same heat treatment (drying at 200 °C for 10 min and annealing at 450 °C for 30 min) to form the SiO₂ xerogel film. Then, a double-xerogel layer, BaTiO₃:(Er, Yb), referred to as the "active cavity layer," was formed from sol II by sequential deposition, followed by annealing at 450 °C for 30 min. Thus, the microcavity structure with an active layer of BaTiO₃:(Er,Yb), which was separated with the undoped SiO₂/BaTiO₃ Bragg reflectors, was fabricated, and it included a lower Bragg reflector consisting of 4 pairs of undoped BaTiO₃ and SiO₂ layers, a thicker (active) double-layer of BaTiO₃:(Er,Yb), and an upper Bragg reflector, which also consisted of 4 SiO₂/BaTiO₃ pairs of undoped layers (Figure 1a). The fabricated sample with a microcavity was separated into two parts, and finally, one part with a microcavity structure was additionally annealed at 800 °C for 30 min.

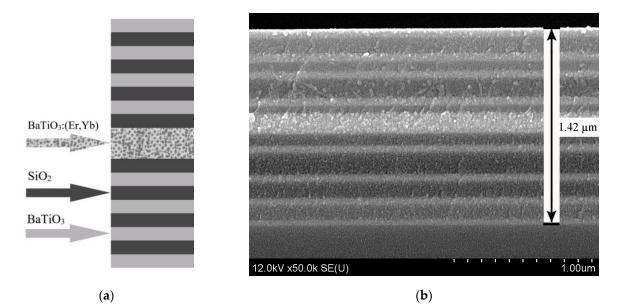


Figure 1. (a) Scheme of the microcavity BaTiO₃: (Er,Yb)/SiO₂ structure and (b) its SEM image after the heat treatment at 450 $^{\circ}$ C.

Two layers of BaTiO₃:(Er, Yb) xerogel were sequentially fabricated on a similar silicon substrate as the reference sample. After spinning, the first layer was annealed at 200 °C for 10 min and then again at 450 °C for 30 min. After that, the second layer was fabricated in the same way. Finally, this double-layer structure was annealed at 450 °C for five hours and then again at 800 °C for 30 min; thus, the heat treatment and thickness of this film corresponded to the heat treatment and thickness of the microcavity BaTiO₃:(Er,Yb) active layer.

Additionally, one layer of $BaTiO_3$:(Er, Yb) xerogel was fabricated on fused silica substrates by spinning and drying, followed by annealing at either 450 or 800 °C for 30 min to analyze the influence of the heat treatment on the optical characteristics of a single $BaTiO_3$:(Er, Yb) xerogel layer.

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2.2. BaTiO₃ Target

Because the expensive components contained Er and Yb, we used two types of powder: a BaTiO₃ xerogel powder undoped with lanthanides, prepared from sol I, and a BaTiO₃:(Er,Yb) xerogel powder prepared from sol II. The xerogel powders were annealed at 1000 °C for 30 min in air. The target was compacted by pulses from a planar impact wave generator with a detonation rate of ~4000 m/s. The developed explosive compaction method produced a planar detonation front that allowed for mixing the upper layers to be significantly reduced and the faceting of the formed target to be improved. A target form with a diameter of 48 mm and a thickness of 4 mm was formed from the BaTiO₃ xerogel powders. Thus, the top part of the target (the front side) was enriched with Er and Yb, whereas the bottom side was depleted with lanthanides.

2.3. Structural and Optical Studies

The morphologies of the obtained samples were studied using a Hitachi S-4800 scanning electron microscope (SEM) (Hitachi, Tokyo, Japan) equipped with a Bruker Quantax 200 spectrometer (Bruker, Berlin, Germany) for the energy dispersive X-ray analyses (EDX).

Studies of the upconversion photoluminescence were carried out under continuouswave (CW) or pulsed optical excitation. A focused 980 nm laser beam of a 200 mW diode module was used for the excitation of the upconversion PL (power density J ~10 W/cm²) in the CW mode. The emission in the visible range was focused on the entrance slit of a 0.6 m grating spectrometer equipped with 1200 gr/mm gratings, and the PL intensity was measured using a R 9110 Hamamatsu photomultiplier tube that was sensitive in the spectral range of 200–850 nm. The spectral resolution of the PL measurement system was ~0.6 nm. A lock-in-amplifier with mechanical chopping at a frequency of approximately 20 Hz was used for the signal recovery.

The time-resolved upconversion PL spectra were measured using an optical parametric oscillator (OPO) (Newport, CA, USA) pumped with the third harmonic (355 nm) of a pulsed Nd:YAG laser and tuned in the spectral range of 700 to 1600 nm. The OPO pulse duration was 10 ns, the repetition rate was 10 Hz, and the average power was ~5 mW. Registration of the upconversion PL in the visible range was carried out using an Acton 2300i (Princeton instruments, Trenton, NJ, USA) grating spectrometer, an Si-based PMT (350–800 nm), and a LeCroy digital oscilloscope (LeCroy, New York, NY, USA).

The spectra of the optical reflection and transmission of the prepared samples were measured using a Cary-500 ScanUV-VIS-NIR spectrophotometer (Varian, Mulgrave, Australia) and an MS122 spectrophotometer (PROSCAN Special Instruments, Minsk, Belarus).

The spectra of the reflection in the temperature range of 26-120 °C were measured using an Ocean Optics USB2000+ spectrometer (Ocean Optics, Dunedin, FL, USA) equipped with a fiber reflection probe and a halogen lamp. During the measurements, the samples were placed horizontally on the heating table, and the sample surface temperatures were monitored by a thermocouple.

The X-ray diffraction (XRD) studies of the target were carried out with a DRON-3 diffractometer (Burevestnik, Leningrad, USSR) using monochromatic Cu K*a* radiation with an exposition of 2 s per 0.04° step at room temperature.

The Raman spectra were recorded using a SOL Instruments Confotec NR500 3D scanning laser Raman spectrometer (SOL Instruments, Minsk, Belarus) with a 473 nm laser diode as the source.

3. Results and Discussion

Figure 1 illustrates the scheme of the fabricated $BaTiO_3:(Er,Yb)/SiO_2$ microcavity and its SEM image after annealing at 450 °C. The image shows a microcavity with an overall thickness of approximately 1.4 µm and a $BaTiO_3:(Er,Yb)$ active layer thickness of approximately 150 nm. Table 1 displays the EDX data of the BaTiO₃:(Er,Yb) target prepared from the same sol (sol II) as the cavity layer. The data were collected from the lanthanide-enriched front side of the target.

Table 1. Chemical composition of the lanthanide-enriched front side of the target determined from the EDX-analysis data averaged from five points of the target's surface.

Element	Concentration, at. %	Standard Deviation, at. %
0	55.6	0.6
Ti	19.0	0.8
Ba	16.6	0.8
С	5.4	0.6
Yb	2.8	0.2
Er	0.6	0.1

According to the EDX studies of the BaTiO₃:(Er,Yb) target, the average total concentration of Er and Yb was 3.4 at. % with the ratio Er:Yb \approx 1:5 and standard deviations of 0.1 at. % for the Er and 0.2 at. % for the Yb.

The XRD spectrum of the BaTiO₃ (Er:Yb)/BaTiO₃ target (Figure 2a) consisted of both the lines related to the BaTiO₃ and additional lines that could be attributed to the phase "A". The numbers represent the perovskite BaTiO₃ lines' *hkl* indices while the letter "A" stands for the lines' "A" phases. It could be seen that the crystalline structure of the target was a cubic perovskite lattice with a cell parameter of approximately 4.009 Å. The absence of splitting of the 200 reflections into tetragonal 002/200 reflections supported our assumptions about the cubic structure of the BaTiO₃. The phase marked "A" on the X-ray diffraction pattern could be attributed to the Er₂O₃, along with the cubic structure of the *Fm*3*m* (225) space group, similar to the results for rare earth oxide thin films [15], though their cell parameters are somewhat smaller than those in this paper.

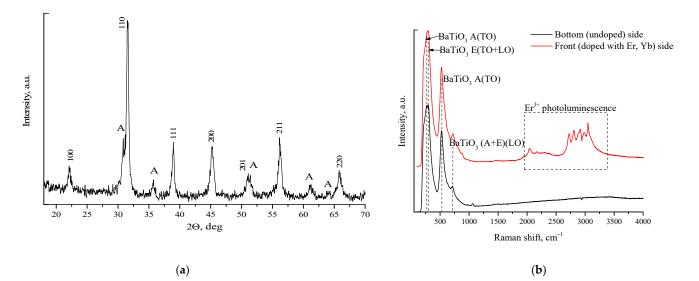
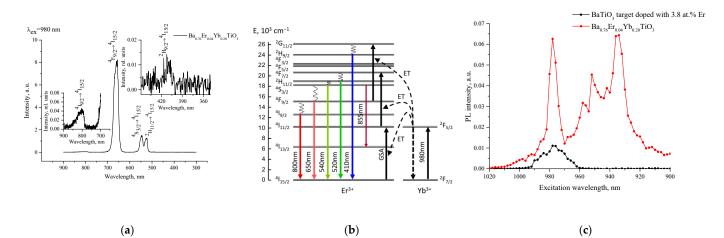


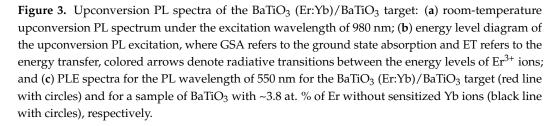
Figure 2. XRD and Raman spectroscopic characterizations of the BaTiO₃ (Er:Yb)/BaTiO₃ target: (a) XRD angular spectrum; and (b) Raman spectra from the front (red line) and bottom (black line) sides of the target.

The Raman spectra recorded from both sides of the target revealed the characteristic lines at 260, 293, 521, and 725 cm⁻¹ (Figure 2b), corresponding to the three major vibration modes of crystalline BaTiO₃ (A(TO), E(TO-LO), and (A + E)(LO)) [16]. The spectra recorded from the front side enriched with the lanthanides showed an additional set of lines in the range of 1900–3000 cm⁻¹, which was associated with the photoluminescence of the

trivalent Er ions excited by the 473 nm laser line. The obtained spectra confirmed both the $BaTiO_3$ crystalline phase and the presence of trivalent erbium ions in the target.

Being excited at 980 nm the front side of the target exhibited bright orange roomtemperature upconversion PL, with the main bands at 410, 523, 546, and 658 nm (Figure 3a,b), which were related to the ${}^{2}\text{H}_{9/2} \rightarrow {}^{4}\text{I}_{15/2}$, ${}^{2}\text{H}_{11/2} \rightarrow {}^{4}\text{I}_{15/2}$, ${}^{4}\text{S}_{3/2} \rightarrow {}^{4}\text{I}_{15/2}$, and ${}^{4}\text{F}_{9/2} \rightarrow {}^{4}\text{I}_{15/2}$ transitions in the Er³⁺ ions, respectively. These upconversion luminescence bands were also observed in the diverse matrices doped with erbium and ytterbium, e.g., CaIn₂O₄, CaGd₂ (WO₄)₄, and Li_xNa_{1-x}CaLa_{0.5} (MoO₄)₃ [17–19].





The upconversion PL intensity was stable and efficient during storage of the target in room-temperature conditions for one year. The PL intensity was approximately six times higher compared to the previously fabricated BaTiO₃ target doped with ~3.8 at. % of Er without sensitized Yb ions, as described in [20]. Figure 3c shows the PL excitation (PLE) spectrum of the BaTiO₃:(Er,Yb) target. We assumed that the relatively broad PLE spectrum within the range of excitation wavelengths 935–980 nm corresponded to a high absorption cross-section of Yb³⁺ ions [21], and that it was a result of the Stark splitting of the Yb³⁺ energy levels in the fabricated BaTiO₃:(Er,Yb) target.

An enhancement of the upconversion PL was observed in the BaTiO₃: (Er,Yb)/SiO₂ microcavity structure in comparison with that in the BaTiO₃:(Er,Yb) film (Figure 4). The upconversion PL from the BaTiO₃:(Er,Yb) layer surrounded with the SiO₂/BaTiO₃ Bragg reflectors was approximately 40 times higher than that of the BaTiO₃:(Er,Yb) layer of approximately the same thickness that was subjected to the same heating method. This result confirmed the earlier reports on the enhanced PL of lanthanides from microcavities prepared using vacuum deposition [22], electrochemistry [23], or the sol-gel method [11,24,25]. The inset of Figure 4 represents the upconversion PL spectrum of the microcavity annealed at 450 °C. The microcavity structure annealed at 450 °C was 360 times weaker compared with the microcavity structure annealed at 800 °C. In contrast to the microcavity structure, no upconversion PL in the BaTiO₃:(Er, Yb) double layer on the silicon annealed at 450 °C was observed (not shown).

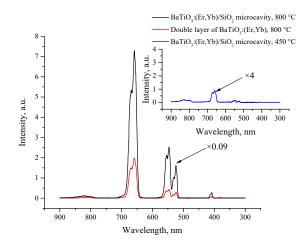
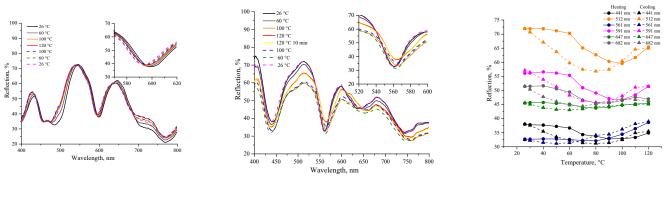


Figure 4. Room-temperature upconversion PL spectra of the BaTiO₃:(Er,Yb)/SiO₂ microcavity (black curve) and the double-layer BaTiO₃:(Er,Yb) structure (red curve) on a silicon substrate after annealing at 800 °C. the inset depicts the spectrum of the upconversion PL of the microcavity (blue curve) after annealing at 450 °C.

Figure 5a,b shows the reflection spectra of the microcavities recorded at different temperatures. Unlike the microcavity fabricated at 450 °C on a fused silica substrate (reported earlier) [10], the high temperature annealing of the microcavity at 800 °C revealed two results. First, the shift in the cavity mode was not as pronounced after annealing the microcavity at a lower temperature, namely, 450 °C [10]. Second, there was a significant deviation in the reflection maxima, e.g., at 512 nm, of the microcavity annealed at 800 °C. The corresponding reflection values changed within 15% in the temperature range of measurements from 25 to 120 °C (Figure 5c).



(a)

(b)

(c)

Figure 5. (a) Reflection spectra of the BaTiO₃:(Er,Yb)/SiO₂ microcavity annealed at 450 °C, measured in the temperature range of 26–130 °C during heating (solid lines), followed by cooling (dashed lines), while the inset shows a selected enlarged region of these spectra. (b) Reflection spectra of the same microcavity after annealing at 800 °C, measured at different temperatures during heating (solid lines), followed by cooling (dashed lines), while the inset shows a selected enlarged region of these spectra. (c) Reflection data for the chosen wavelengths for the sample annealed at 800 °C for one cycle of heating (circles with solid lines), followed by cooling (triangles with dashed lines).

The prepared target appeared to be useful for potential applications as an IR laser radiation visualizer and for the production of $BaTiO_3$ film structures by sputtering in a vacuum. The effect of sample temperature on the amplitude of the reflection spectrum, as well as an intense upconversion luminescence for structures treated at 800 °C, and the previously noted shift of the cavity mode for the less-dense xerogel structures treated at

 $450 \,^{\circ}$ C [10] encourage further research into the characteristics of barium titanate structures doped with lanthanides for optical adsorption and for use as temperature sensors and remote monitoring systems [26–28].

Further, on the basis of the measured reflections and transmission spectra of the singlelayer BaTiO₃:(Er,Yb) films annealed either at 450 or 800 °C on a plane-parallel dielectric substrate of finite thickness, we calculated the complex refractive index N = n - ik of the BaTiO₃:(Er,Yb) by optimizing the parameters of the Lagrange–Chebyshev polynomial fit (for the details of solving the inverse spectrometry problem, see [29]). The following physical values for these two single-layer BaTiO₃:(Er,Yb) films annealed at 450 or 800 °C were determined from the reflections and transmission spectra: n, k, E_g , and E_u , where nis the real part of the refractive index of the film, k is the imaginary part of the refractive index or absorption index, E_g is the optical band gap, and E_u is the Urbach energy.

The obtained solution of the inverse spectrophotometry problem provided the results presented in Figures 6–8. Figure 6 depicts the reflection and transmission spectra of the single-layer BaTiO₃:(Er,Yb) films deposited on the fused silica substrates and annealed at 450 or 800 °C. The triangles and circles represent the experimental points, and the solid lines are the calculated spectra. Figure 7 shows the calculated spectra of the refractive index *n* (Figure 7a) and the absorption index *k* (Figure 7b) for a single-layer BaTiO₃:(Er,Yb) film annealed at 450 and 800 °C. The discrepancy χ between the measured and calculated data satisfied the criterion $\chi^2 \ll 1$. The thickness of the single-layer film annealed at 450 °C was 99 nm and that of the film annealed at 800 °C was 65 nm. The higher annealing temperature led to a decrease in the BaTiO₃:(Er,Yb) films, and that for the undoped BaTiO₃ films was confirmed by means of SEM in [9,10]. The decrease in the film thickness meant an increase in the film density ρ , which could lead to a larger refractive index, in accordance with the Lorentz–Lorenz formula $(n^2 - 1)/(n^2 + 1) \sim \rho$ [30].

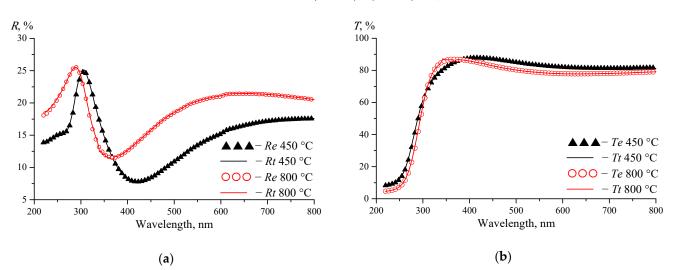


Figure 6. (a) Reflection and (b) transmission spectra of the single-layer BaTiO₃:(Er,Yb) films deposited on fused silica substrates annealed at 450 and 800 °C. The triangles and circles represent the experimental data of the transmission (T_e) and reflection (R_e), and the solid lines are the calculated transmission (T_t) and reflection (R_t) spectra.

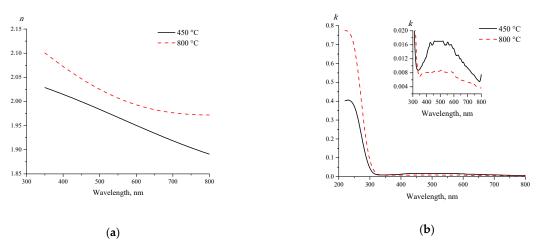


Figure 7. (a) Spectra of the refractive index *n* and (b) the absorption index *k* for the two BaTiO₃: (Er,Yb) films annealed at 450 and 800 $^{\circ}$ C.

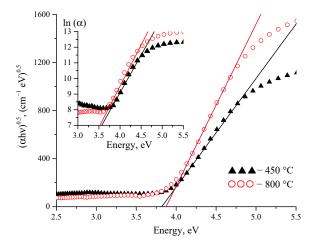


Figure 8. Estimation of the optical band gap and the Urbach energy for the indirect transitions in the BaTiO₃:(Er,Yb) films annealed at 450 and 800 °C.

The higher reflectivity in the spectral region from 400 to 800 nm (Figure 6a) corresponded to the relatively low absorption (Figure 7b) that resulted in the lower transmittance (Figure 6b) for the film annealed at 800 °C in comparison with that of the film annealed at 450 °C.

In Figure 7b, in the UV range, the maximum of $k(\lambda)$ for the film annealed at 800 °C was two times higher than that for the film annealed at 450 °C, while in the visible range, the maximum of $k(\lambda)$ was two times lower than that for the film annealed at 450 °C. The increase in the refractive index *n* (Figure 7a) with the increase in the annealing temperature of the film resulted in significant increases in their reflectivity *R* (Figure 6a). Large losses of light energy due to the reflection and small losses due to the absorption (Figure 7b) led to decreases in the transmittance *T* in the visible and near-IR regions with the increase in the annealing temperature. In fact, BaTiO₃ is known to be an appealing host of lanthanides for the UV excitation of visible luminescence [11], as well as an appealing transparent coating for UV filters and solar cells for the prevention of thermalization.

Then we calculated the absorption coefficient $\alpha(\lambda)$ using the following formula:

$$\alpha(\lambda) = \frac{4\pi k(\lambda)}{\lambda 10^{-7}},\tag{1}$$

and the Tauc extrapolation [31] is used as follows:

$$[\alpha(\lambda)E]^m = B(E - E_g), \tag{2}$$

to determine the optical band gaps of the BaTiO₃: (Er,Yb) films.

In Formula (2), *B* is a constant, $E = 1240 \lambda^{-1}$ is the photon energy in eV, and the wavelength λ is taken in nm. The intersection of the linear range of the dependence $[\alpha(\lambda)E]^m$ with the *E* axis yields the estimated value of E_g . The estimation of the optical band gap is given in Figure 8 by assuming the indirect optical transition (m = 0.5). We concluded that $E_g = 3.82$ eV for the film annealed at 450 °C, while it was approximately 3.87 eV for the film annealed at 800 °C.

The Urbach energy is determined by analyzing the plot of $\ln (\alpha(E))$, as shown in the inset of Figure 8. In this case, the following function:

$$f(E) = \ln\left(\alpha\left(1240E_g^{-1}\right)\exp\left((E - E_g)E_u^{-1}\right)\right),\tag{3}$$

is linear and must pass through the corresponding points of the function $\ln(\alpha(E))$.

An analysis of the absorption spectra shown in Figure 7b by using Formula (3) allowed us to estimate $E_u = 0.21$ eV and 0.16 eV for the films annealed at 450 °C and 800 °C, respectively. The lower Urbach energy for the higher annealing temperature could be explained by a decrease in the crystal lattice disorder in the nanocrystalline BaTiO₃ film. In fact, the Urbach tail states, which provide information about various disorders related to the random distribution of both intrinsic atoms and impurities [32–34], should decrease with an increase in the annealing temperature because the contribution of the amorphous phase becomes smaller. This fact was also proved by the increase in absorption in the high energy region, as shown in Figures 7 and 8.

The estimated optical band gaps for our samples were comparable to the data for the undoped 300-nm-thick BaTiO₃ films with a grain size of approximately 95 nm that were produced using pulsed laser deposition and had an optical band gap of 3.77 eV [34]. The difference in the optical band gap measured for thin films generated in the present work as well as in Ref. [34] and for the solution-grown crystals of BaTiO₃ (3.38 and 3.27 eV, respectively, for two directions of the light polarization [35]) could be explained by considering the quantum confinement for charge carriers in low-dimensional BaTiO₃ films and nanocrystalline structures [36,37]. According to Suzuki and Kijima [37], the band gap of BaTiO₃ was estimated to be at a constant value of approximately 3.2 eV for the BaTiO₃ particles larger than 15 nm, which is in agreement with the data reported by Wemple [33] for a BaTiO₃ crystal, and E_g gradually increased as the particle sizes smaller than 11.5 nm decreased, and it was approximately 0.25 eV larger than that of the bulk BaTiO₃.

The observed enhancement of the upconversion luminescence in the film annealed at 800 °C could be explained by thermal annealing of the nonradiative centers, which control the population of the excited states of trivalent erbium. The most probable candidates are the intrinsic defect states in the band gap of the barium titanate matrix, which are detectable as the Urbach tail states in the absorption spectra (Figure 8), and the hydroxyl groups, which are known to be responsible for the quenching of the erbium luminescence in oxide matrices [38]. The higher annealing temperature resulted in the lower efficiencies of both quenching processes in the investigated samples.

4. Conclusions

Colloidal solutions for the synthesis of $BaTiO_3$ xerogel doped with Er and Yb ($Ba_{0.76}Er_{0.04}Yb_{0.20}TiO_3$) were used for the fabrication of a sol-gel-derived target using the explosive compaction method and a spin-on deposited multilayer microcavity structure ($BaTiO_3:(Er,Yb)/SiO_2$ microcavity), demonstrating the strong room-temperature upconversion photoluminescence of trivalent erbium ions. The $BaTiO_3:(Er,Yb)/SiO_2$ microcavity exhibited a significant increase in upconversion photoluminescence when compared to the $BaTiO_3:(Er,Yb)$ double-layer that was fabricated directly on silicon. The

enhanced upconversion photoluminescence was also observed in the microcavity structure annealed at 800 °C. The reflection spectra of the BaTiO₃:(Er, Yb)/SiO₂ microcavity annealed at 800 °C demonstrated a deviation in the maxima of the reflection spectra within 15% for the temperature range of 26–120 °C. From the analysis of the transmission and reflection spectra, we determined that, for the single layer of BaTiO₃:(Er,Yb) spin-on film annealed at 450 °C, the optical band gap for indirect electron transitions was $E_g = 3.82$ eV, while for the film annealed at 800 °C, it was equal to $E_g = 3.87$ eV. The results obtained demonstrate new possibilities for tuning the optical properties and efficiencies of the upconversion luminescence of rare-earth-doped sol-gel materials and structures for photonic applications.

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References

- 1. Karvounis, A.; Timpu, F.; Vogler-Neuling, V.V.; Savo, R.; Grange, R. Barium titanate nanostructures and thin films for photonics. *Adv. Opt. Mater.* **2020**, *8*, 2001249. [CrossRef]
- Strek, W.; Hreniak, D.; Boulon, G.; Guyot, Y.; Pazik, R. Optical behavior of Eu³⁺-doped BaTiO₃ nano-crystallites prepared by sol–gel method. *Opt. Mater.* 2003, 24, 15–22. [CrossRef]
- 3. Kumari, M.; Yadav, A.; Sarun, P.M. Systematic investigation of structural, optical and dielectric properties of 0.5 mol% Eu:BaTiO₃ ceramics. *Mater. Today Proc.* **2020**, *46*, 6102–6106. [CrossRef]
- Jia, Q.X.; Shi, Z.Q.; Anderson, W.A. BaTiO₃ thin film capacitors deposited by r.f. magnetron sputtering. *Thin Solid Films* 1992, 209, 230–239. [CrossRef]
- Petraru, A.; Schubert, J.; Schmid, M.; Buchal, C. Ferroelectric BaTiO₃ thin-film optical waveguide modulators. *Appl. Phys. Lett.* 2002, *81*, 1375–1377. [CrossRef]
- Tang, P.; Towner, D.; Hamano, T.; Meier, A.; Wessels, B. Electrooptic modulation up to 40 GHz in a barium titanate thin film waveguide modulator. *Opt. Express* 2004, 12, 5962–5967. [CrossRef]
- Subasri, R.; Reddy, D.S.; Soma Raju, K.R.C.; Rao, K.S.; Kholov, P.; Gaponenko, N. Sol–gel derived Ba/SrTiO₃–MgF₂ solar control coating stack on glass for architectural and automobile applications. *Res. Chem. Intermed.* 2019, 45, 4179–4191. [CrossRef]
- 8. Zhou, J.; Sun, C.Q.; Pita, K.; Lam, Y.L.; Zhou, Y.; Ng, S.L.; Kam, C.H.; Li, L.T.; Gui, Z.L. Thermally tuning of the photonic band gap of SiO₂ colloid-crystal infilled with ferroelectric BaTiO₃. *Appl. Phys. Lett.* **2001**, *78*, 661–663. [CrossRef]
- 9. Gaponenko, N.V.; Kholov, P.A.; Sukalin, K.S.; Raichenok, T.F.; Tikhomirov, S.A.; Subasri, R.; Soma Raju, K.R.C.; Mudryi, A.V. Optical properties of multilayer BaTiO₃/SiO₂ film structures formed by the sol–gel method. *Phys. Solid State* **2019**, *61*, 397–401. [CrossRef]
- Lashkovskaya, E.I.; Gaponenko, N.V.; Stepikhova, M.V.; Yablonskiy, A.N.; Andreev, B.A.; Zhivulko, V.D.; Mudryi, A.V.; Martynov, I.L.; Chistyakov, A.A.; Kargin, N.I.; et al. Optical properties and upconversion luminescence of BaTiO₃ xerogel structures doped with erbium and ytterbium. *Gels* 2022, *8*, 347. [CrossRef]

- 11. Gaponenko, N.V.; Kholov, P.A.; Raichenok, T.F.; Prislopski, S.Y. Enhanced luminescence of europium in sol-gel derived BaTiO₃/SiO₂ multilayer cavity structure. *Opt. Mater.* **2019**, *96C*, 109265–109269. [CrossRef]
- 12. Ghosh, P.; Sadhu, S.; Sen, T.; Patra, A. Upconversion emission of BaTiO₃:Er nanocrystals. Bull. Mater. Sci. 2008, 31, 461–465. [CrossRef]
- Chen, L.; Wei, X.; Fu, X. Effect of Er substituting sites on upconversion luminescence of Er³⁺-doped BaTiO₃ films. *Trans. Nonferr. Met. Soc. China* 2012, 22, 1156–1160. [CrossRef]
- Bae, H.; Lee, E.; Lee, K.T. Power-dependent photophysical pathways of upconversion in BaTiO₃:Er³⁺. *Phys. Chem. Chem. Phys.* 2021, 23, 14587–14591. [CrossRef] [PubMed]
- 15. Kashaev, A.A.; Ushchapovskii, L.V.; Il'in, A.G. Electron-diffraction and X-ray diffraction study of rare earth metal oxides in thin films. *Sov. Phys. Crystallogr.* **1975**, *20*, 114–115.
- 16. Parsons, J.L.; Rimai, L. Raman spectrum of BaTiO₃. Solid State Commun. 1967, 5, 423–427. [CrossRef]
- 17. Lim, C.S.; Aleksandrovsky, A.; Molokeev, M.; Oreshonkov, A.; Atuchin, V. Microwave sol–gel synthesis and upconversion photoluminescence properties of CaGd₂(WO₄)4:Er³⁺/Yb³⁺ phosphors with incommensurately modulated structure. *J. Solid State Chem.* **2015**, *228*, 160–166. [CrossRef]
- 18. Liu, M.H.; Li, T.T.; Wang, X.; Liu, D.Y.; Yuan, N.; Zhang, D.L.; Tian, Y. Synthesis and Er³⁺ spectroscopic property of Er³⁺/Yb³⁺- codoped CaIn₂O₄ nano-fibers for thermometry. *J. Lumin.* **2019**, *215*, 116703. [CrossRef]
- Lim, C.S.; Aleksandrovsky, A.; Molokeev, M.; Oreshonkov, A.; Atuchin, V. Structural and spectroscopic effects of Li⁺ substitution for Na⁺ in LixNa_{1-x}CaLa_{0.5}Er_{0.05}Yb_{0.45}(MoO₄)₃ upconversion scheelite-type phosphors. *Crystals* **2023**, *13*, 362. [CrossRef]
- Gaponenko, N.V.; Sudnik, L.V.; Vityaz, P.A.; Luchanok, A.R.; Stepikhova, M.V.; Yablonskiy, A.N.; Lashkovskaya, E.I.; Shustsikava, K.V.; Radyush, Y.V.; Zhivulko, V.D.; et al. Upconversion luminescence of Er³⁺ ions from barium titanate xerogel powder and target fabricated by explosive compaction method. *J. Appl. Spectrosc.* 2022, *89*, 238–243. [CrossRef]
- Tolstik, N.A.; Kurilchik, S.V.; Kisel, V.E.; Kuleshov, N.V.; Maltsev, V.V.; Pilipenko, O.V.; Koporulina, E.V.; Leonyuk, N.I. Efficient 1 W continuous-wave diode-pumped Er,Yb:YAl₃(BO₃)₄ laser. *Opt. Lett.* 2007, *32*, 3233–3235. [CrossRef] [PubMed]
- Schubert, E.F.; Vredenberg, A.M.; Hunt, N.E.J.; Wong, Y.H.; Becker, P.C.; Poate, J.M.; Jacobson, D.C.; Feldman, L.C.; Zydzik, G.J. Giant enhancement of luminescence intensity in Er-doped Si/SiO₂ resonant cavities. *Appl. Phys. Lett.* **1992**, *61*, 1381–1383. [CrossRef]
- Lopez, H.A.; Fauchet, P.M. Erbium emission from porous silicon one-dimensional photonic band gap structures. *Appl. Phys. Lett.* 2000, 77, 3704–3706. [CrossRef]
- 24. Bellessa, J.; Rabaste, S.; Plenet, J.C.; Dumas, J.; Mugnier, J.; Marty, O. Eu³⁺-doped microcavities fabricated by sol–gel process. *Appl. Phys. Lett.* **2001**, *79*, 2142–2144. [CrossRef]
- Rojas-Hernandez, R.E.; Santos, L.F.; Almeida, R.M. Photonic crystal assisted up-converter based on Tb³⁺/Yb³⁺-doped aluminosilicate glass. *Opt. Mater.* 2018, 83, 61–67. [CrossRef]
- 26. Mitschke, F. Fiber-optic sensor for humidity. Opt. Lett. 1989, 14, 967–969. [CrossRef]
- 27. Tripathy, A.; Pramanik, S.; Cho, J.; Santhosh, J.; Abu Osman, N.A. Role of morphological structure, doping, and coating of different materials in the sensing characteristics of humidity sensors. *Sensors* 2014, 14, 16343–16422. [CrossRef] [PubMed]
- 28. Ryszczyńska, S.; Trejgis, K.; Marciniak, Ł.; Grzyb, T. Upconverting SrF₂:Er³⁺ Nanoparticles for Optical Temperature Sensors. *ACS Appl. Nano Mater.* **2021**, *4*, 10438–10448. [CrossRef]
- Sotsky, A.B.; Mikheev, S.S.; Stas'kov, N.I.; Sotskaya, L.I. Spectrophotometry of Layers on Plane Parallel Substrates. *Opt. Spectrosc.* 2020, 128, 1155–1166. [CrossRef]
- 30. Born, M.; Wolf, E. *Principles of Optics: Electromagnetic Theory of Propagation, Interference and Diffraction of Light*, 6th ed.; Elsevier: Amsterdam, The Netherlands, 2013.
- Tauc, J.; Grigorovici, R.; Vancu, A. Optical properties and electronic structure of amorphous germanium. *Phys. Status Solidi* 1966, 15, 627–637. [CrossRef]
- Mishra, V.; Sagdeo, A.; Kumar, V.; Warshi, M.K.; Rai, H.M.; Saxena, S.K.; Roy, D.R.; Mishra, V.; Kumar, R.; Sagdeo, P.R. Electronic and optical properties of BaTiO₃ across tetragonal to cubic phase transition: An experimental and theoretical investigation. *J. Appl. Phys.* 2017, 122, 065105. [CrossRef]
- Borah, M.; Mohanta, D. Effect of Gd³⁺ doping on structural, optical and frequency-dependent dielectric response properties of pseudo-cubic BaTiO₃ nanostructures. *Appl. Phys. A* 2014, 115, 1057–1067. [CrossRef]
- Ahadi, K.; Mahdavi, S.M.; Nemati, A.; Tabesh, M.; Ranjbar, M. Electronic structure and morphological study of BaTiO₃ film grown by pulsed-laser deposition. *Mater. Lett.* 2012, 72, 107–109. [CrossRef]
- 35. Wemple, S.H. Polarization fluctuations and the optical-absorption edge in BaTiO₃. Phys. Rev. B 1970, 2, 2679–2689. [CrossRef]
- 36. Cullis, A.; Canham, L. Visible light emission due to quantum size effects in highly porous crystalline silicon. *Nature* **1991**, *353*, 335–338. [CrossRef]
- Suzuki, K.; Kijima, K. Optical band gap of barium titanate nanoparticles prepared by RF-plasma chemical vapor deposition. *Jpn. J. Appl. Phys.* 2005, 44, 2081–2082. [CrossRef]
- Yan, Y.; Faber, A.J.; de Waal, H. Luminescence quenching by OH groups in highly Er-doped phosphate glasses. J. Non-Cryst. Solids 1995, 181, 283–290. [CrossRef]

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